

*"Broadening the knowledge base and supporting the long term professional sustainability of the Research University Centre of Excellence at the University of Szeged by ensuring the rising generation of excellent scientists."*



# Doctoral School of Mathematics and Computer Science

## Stochastic Days in Szeged

26.07.2012.

My collaboration with András:  
mathematical and human excerpts

**Domokos Szász**

(Budapest University of Technology and Economics)



TÁMOP-4.2.2/B-10/1-2010-0012 project



# My collaboration with András

## Mathematical and human excerpts

**Domokos Szász**

Budapest University of Technology

**András is 70**

Szeged, 2013, July 26

## 1969-70, Moscow: Acquaintance with András

The Hungarian gang: András, Mályusz, Szemerédi and other grads and undergrads.

Late night walks in the woods around Lomonosov University. Exchanging ideas what we had heard, learnt, and also about everything, in general.

Great concerts.

Playing the recorder: Bach, Schubert, Mozart, Bartók, Haydn, etc.

A moment: Mályusz writing the notes of Iván Szenes's "Kislány a zongoránál" (Winner of Dance Song Festival, 1968) onto the door of wardrobe of my room, and by Mályusz himself directing our blockflöte duo: alto and soprano.

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A semi-phenomenological model à la Eckmann-Young and Lin-Young

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Highly intellectual and cultured, absolutely cosmopolitan, most clearly and originally thinking and living, enthusiastic and warm personality.

Strong influence on all he has contact with.

Impressionists (Vienna, Spanische Reiterschule: Renoir)

Schnittke, Janacek

# Musil: The Man without Qualities (1930-42).

... man erhält eine stationäre Reihe oder eine **Verteilungsfunktion**, man berechnet das Mass der Schwankung, die **mittlere Abweichung**, das Mass der Abweichung von einem beliebigen Wert, **den Zentralwert**, den Normalwert, den Durchschnittswert, **die Dispersion** und so weiter und untersucht mit allen solchen Begriffen das gegebene Vorkommen.

Sie kennen sicher diese Beispiele aus irgendeiner Vorlesung über Gesellschaftslehre. Etwa **die Statistik der Ehescheidungen in Amerika**. Oder **das Verhältnis zwischen Knaben- und Mädchengeburten**, das ja eine der konstantesten Verhältniszahlen ist.

Man nennt das etwas schleierhaft **das Gesetz der großen Zahlen**. Ich mache Ihnen einen Vorschlag, Gerda. Nehmen wir an, dass es im Moralischen genau so zugehe wie **in der kinetischen Gastheorie**: alles fliegt regellos durcheinander, jedes macht, was es will, aber wenn man berechnet, was sozusagen keinen Grund hat, daraus zu entstehen, so ist es gerade das, was **wirklich entsteht!**

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